

Chapter 34 Problem 41 [†]

Given

$$\lambda_{max} = 558 \text{ nm}$$

Solution

- a) What is the temperature of the blackbody?

Using Wein's law

$$\lambda_{peak} T = 2.898 \times 10^{-3} \text{ m} \cdot K$$

$$T = \frac{2.898 \times 10^{-3} \text{ m} \cdot K}{\lambda_{peak}} = \frac{2.898 \times 10^{-3} \text{ m} \cdot K}{558 \times 10^{-9}} = 5190 \text{ K}$$

- b) What is the ratio of radiance at 382 nm compared to 694 nm?

The radiance formula for a blackbody radiator is

$$R(\lambda, T) = \frac{2\pi hc^2}{\lambda^5 (e^{hc/\lambda kT} - 1)}$$

The radiance at 382 nm is

$$R(382 \text{ nm}, 5190 \text{ K}) = \frac{2\pi (6.63 \times 10^{-34} \text{ J} \cdot \text{s})(3.0 \times 10^8 \text{ m/s})^2}{(382 \times 10^{-9} \text{ m})^5 (e^{(6.63 \times 10^{-34} \text{ J} \cdot \text{s})(3.0 \times 10^8 \text{ m/s}) / ((382 \times 10^{-9} \text{ m})(1.38 \times 10^{-23} \text{ J/K})(5190 \text{ K}))} - 1)$$

$$R(382 \text{ nm}, 5190 \text{ K}) = 3.23 \times 10^{13}$$

The radiance at 694 nm is

$$R(694 \text{ nm}, 5190 \text{ K}) = \frac{2\pi (6.63 \times 10^{-34} \text{ J} \cdot \text{s})(3.0 \times 10^8 \text{ m/s})^2}{(694 \times 10^{-9} \text{ m})^5 (e^{(6.63 \times 10^{-34} \text{ J} \cdot \text{s})(3.0 \times 10^8 \text{ m/s}) / ((694 \times 10^{-9} \text{ m})(1.38 \times 10^{-23} \text{ J/K})(5190 \text{ K}))} - 1)$$

$$R(694 \text{ nm}, 5190 \text{ K}) = 4.35 \times 10^{13}$$

The ratio of the two radiance is then

$$\frac{R(382 \text{ nm}, 5190 \text{ K})}{R(694 \text{ nm}, 5190 \text{ K})} = \frac{3.23 \times 10^{13}}{4.35 \times 10^{13}} = 0.743$$

[†]Problem from Essential University Physics, Wolfson