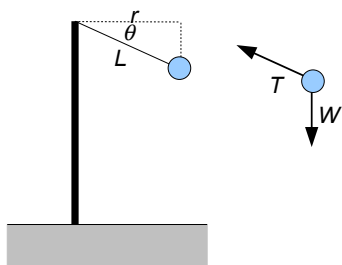


Chapter 5 Problem 28 †



Given

$$L = 1.55 \text{ m}$$

$$\theta = 12.0^\circ$$

Solution

Find the speed of the tetherball.

Using the free-body diagram given above and Newton's 2nd law gives

$$\Sigma \vec{F} = m\vec{a}$$

$$\vec{T} + \vec{W} = m\vec{a}$$

Making the x direction horizontal and resolving into unit vector notation gives

$$-T \cos \theta \hat{i} + T \sin \theta \hat{j} - mg \hat{j} = m\vec{a}$$

Now the ball is experiencing centripetal acceleration because it is moving at constant speed at a radius of r. This acceleration is in the $-x$ direction. The equation becomes

$$-T \cos \theta \hat{i} + T \sin \theta \hat{j} - mg \hat{j} = -ma \hat{i}$$

The x-component equation is

$$-T \cos \theta = -ma \tag{1}$$

and the y-component equation is

$$T \sin \theta - mg = 0 \tag{2}$$

Use equation (2) and solve for T.

$$T = \frac{mg}{\sin \theta}$$

Substitute this into equation (1) and solve for a.

$$-\left(\frac{mg}{\sin \theta}\right) \cos \theta = -ma$$

$$\frac{mg}{\tan \theta} = ma$$

†Problem from Essential University Physics, Wolfson

$$a = \frac{g}{\tan \theta} = \frac{(9.8 \text{ m/s}^2)}{\tan(12^\circ)} = 46.1 \text{ m/s}^2$$

Since the acceleration is centripetal, then

$$a = \frac{v^2}{r}$$

Solving for speed gives

$$v^2 = ar$$

$$v = \sqrt{ar}$$

(3)

From the diagram notice that r is the adjacent side of the given angle; therefore,

$$r = L \cos \theta$$

and equation (3) becomes

$$v = \sqrt{aL \cos \theta} = \sqrt{(46.1 \text{ m/s}^2)(1.55 \text{ m}) \cos(12^\circ)} = 8.36 \text{ m/s}$$