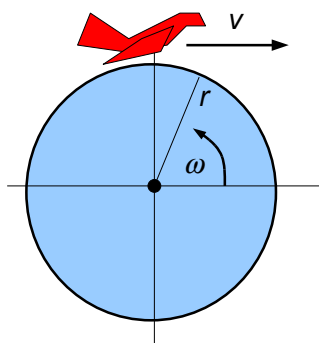


Chapter 11 Problem 43 †



**Given**

$$r = 19 \text{ cm} = 0.19 \text{ m}$$

$$I_f = 0.12 \text{ kg} \cdot \text{m}^2$$

$$\omega_f = 5.6 \text{ rpm}$$

$$m_b = 140 \text{ g} = 0.140 \text{ kg}$$

$$v_b = 1.1 \text{ m/s}$$

**Solution**

Find the rotation rate after the bird lands on the feeder.

First convert the angular velocity of the feeder into radians per second.

$$\omega_f = 5.6 \text{ rev/min} \left( \frac{1 \text{ min}}{60 \text{ s}} \right) \left( \frac{2\pi \text{ rad}}{1 \text{ rev}} \right) = 0.586 \text{ rad/s}$$

Just before the bird lands on the feeder, the moment of inertia of the bird is essentially that of a point mass at a distance  $r$  from the center of the feeder. Therefore,

$$I_b = m_b r^2$$

The angular velocity of the bird just before landing is negative because it is a clockwise rotation relative to the center of the feeder and has a value of

$$\omega_b = -\frac{v_b}{r}$$

The angular momentum of the bird just before landing is then

$$L_b = I_b \omega_b = -m_b r^2 \frac{v_b}{r} = -m_b r v_b$$

The angular momentum of the feeder before the bird lands is

$$L_f = I_f \omega_f$$

After the bird lands, the moment of inertia of bird/feeder combination is

$$I_T = I_b + I_f = m_b r^2 + I_f$$

and the angular momentum after the landing is

$$L_T = I_T \omega_T = (m_b r^2 + I_f) \omega_T$$

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†Problem from Essential University Physics, Wolfson

Using conservation of angular momentum we have

$$L_b + L_f = L_T$$

$$-m_b r v_b + I_f \omega_f = (m_b r^2 + I_f) \omega_T$$

Solving for the angular velocity after the landing gives

$$\omega_T = \frac{-m_b r v_b + I_f \omega_f}{m_b r^2 + I_f}$$

Substitute in the provided values

$$\omega_T = \frac{-(0.140 \text{ kg})(0.19 \text{ m})(1.1 \text{ m/s}) + (0.12 \text{ kg} \cdot \text{m}^2)(0.586 \text{ rad/s})}{(0.140 \text{ kg})(0.19 \text{ m})^2 + 0.12 \text{ kg} \cdot \text{m}^2}$$

$$\omega_T = \frac{-0.0293 \text{ kg} \cdot \text{m}^2/\text{s} + 0.0703 \text{ kg} \cdot \text{m}^2/\text{s}}{0.125 \text{ kg} \cdot \text{m}^2} = 0.328 \text{ rad/s}$$

Converting this into revolutions per minutes gives

$$\omega_T = 0.328 \text{ rad/s} \left( \frac{1 \text{ rev}}{2\pi \text{ rad}} \right) \left( \frac{60 \text{ s}}{1 \text{ min}} \right) = 3.1 \text{ rpm}$$