

Chapter 10 Problem 36 †

Given

$$m = 150 \text{ g} = 0.150 \text{ kg}$$

$$v = 33 \text{ m/s}$$

$$\omega = 42 \text{ rad/s}$$

$$r = 3.7 \text{ cm} = 0.037 \text{ m}$$

Solution

Find the fraction of kinetic energy that is rotational.

Since the baseball is solid, its moment of inertia is

$$I = \frac{2}{5}mr^2 = \frac{2}{5}(0.150 \text{ kg})(0.037 \text{ m})^2 = 8.21 \times 10^{-5} \text{ kg} \cdot \text{m}^2$$

The rotational kinetic energy of the baseball is then

$$K_{rot} = \frac{1}{2}I\omega^2 = \frac{1}{2}(8.21 \times 10^{-5} \text{ kg} \cdot \text{m}^2)(42 \text{ rad/s})^2 = 0.0724 \text{ J}$$

The translational kinetic energy of the baseball is

$$K_{tran} = \frac{1}{2}mv^2 = \frac{1}{2}(0.150 \text{ kg})(33 \text{ m/s})^2 = 81.68 \text{ J}$$

The fraction of kinetic energy in rotation is

$$fraction = \frac{K_{rot}}{K_{tran} + K_{rot}} = \frac{0.0724 \text{ J}}{81.68 \text{ J} + 0.0724 \text{ J}} = 8.86 \times 10^{-4}$$

†Problem from Essential University Physics, Wolfson