Chapter 10 Problem 32 [†]

Given

$$\begin{split} m &= 108 \; g = 0.108 \; kg \\ D &= 24 \; cm = 0.24 \; m \\ \Delta\theta &= 1/4 \; turn = \pi/2 \; rad \\ \Delta\omega &= 550 \; rpm = \left(\frac{550 \; rev}{min}\right) \left(\frac{2\pi \; rad}{rev}\right) \left(\frac{1 \; min}{60 \; s}\right) = 57.6 \; rad/s \end{split}$$

Solution

a) Find the moment of inertia of the Frisbee.

Half of the mass is distributed as a ring with a moment of inertia of $I = MR^2$ and half of the mass is distributed as a disk with a moment of inertia of $I = \frac{1}{2}MR^2$. Therefore, $M = m/2 = 0.054 \ kg$. Also notice that the diameter of the Frisbee is given and we need the radius. The total moment of inertia is then

$$I_{tot} = MR^2 + \frac{1}{2}MR^2 = \frac{3}{2}MR^2 = \frac{3}{2}(0.054 \ kg)(0.12 \ m)^2$$
$$I_{tot} = 1.17 \times 10^{-3} \ kg \cdot m^2$$

b) Find the torque exerted on the Frisbee.

Torque generates an angular acceleration with a magnitude given by the formula

$$\tau = I\alpha \tag{1}$$

The angular acceleration can be derived from the kinematic formula

$$\omega_f^2 - \omega_0^2 = 2\alpha\Delta\theta$$

Solving for α and substituting into equation 1 gives

$$\tau = \frac{I(\omega_f^2 - \omega_0^2)}{2\Delta\theta} = \frac{(1.17 \times 10^{-3} \ kg \cdot m^2)((57.6 \ rad/s)^2 - (0)^2)}{2(\pi/2)}$$

$$\tau = 1.24 \ N \cdot m$$

[†]Problem from Essential University Physics, Wolfson