

Chapter 7

Problem 80

$$\Delta h = 50 \text{ m}$$
$$P = 500 \text{ W}$$

How much coal per minute can be brought to the surface

The ~~one~~ work done to lift an object against gravity is

$$W = mg \Delta h$$

Power is $P = \frac{W}{t}$

so $W = P \cdot t$

Since we are ignoring friction, we are only doing work against gravity. so,

$$P \cdot t = mg \Delta h$$

Solving for mass per time gives

$$\frac{m}{t} = \frac{P}{g \Delta h}$$

Substituting in values gives

$$\frac{m}{t} = \frac{500 \text{ W}}{(9.8 \text{ m/s}^2)(50 \text{ m})} = 1.02 \frac{\text{W}}{\frac{\text{m}}{\text{s}^2} \cdot \text{m}}$$

now watts is ~~J/s~~ $\frac{\text{J}}{\text{s}} = \frac{\text{N} \cdot \text{m}}{\text{s}} = \frac{(\text{kg} \frac{\text{m}}{\text{s}^2}) \cdot \text{m}}{\text{s}} = \text{kg} \frac{\text{m}^2}{\text{s}^3}$

so the units for this answer are

$$\frac{m}{t} = 1.02 \frac{\text{kg} \frac{\text{m}^2}{\text{s}^3}}{\frac{\text{m}^2}{\text{s}^2}} = 1.02 \frac{\text{kg}}{\text{s}}$$

In one minute we have $\frac{m}{t} = 1.02 \frac{\text{kg}}{\text{s}} \left(\frac{60 \text{ s}}{1 \text{ min}} \right) = \boxed{61.2 \text{ kg/min}}$