

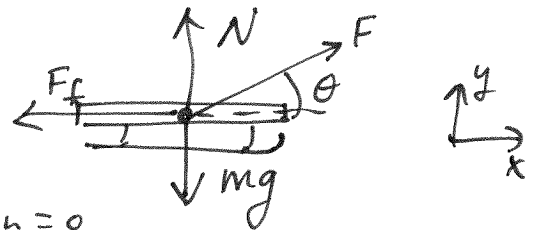
$$\mu_k = 0.20$$

$$m = 50 \text{ kg}$$

$$d = 20 \text{ m}$$

$$\vec{F} = F \angle 25^\circ$$

constant velocity \therefore acceleration = 0



Using Newton's 2nd law

$$\sum \vec{F} = m\vec{a}$$

$$\vec{F}_f + \vec{N} + \vec{F} + \vec{W} = m\vec{a} = 0$$

let horizontal be in the x-direction.

$$-F_f \hat{i} + N \hat{j} + F \cos 25^\circ \hat{i} + F \sin 25^\circ \hat{j} - mg \hat{j} = 0$$

x-dir) $-F_f + F \cos 25 = 0$ (#1)

y-dir) $N + F \sin 25 - mg = 0$ (#2)

$$F_f = \mu N$$
 (#3)

a) Calculate the applied force + work done by this force
sub (#3) into (#1)

$$-\mu N + F \cos 25 = 0 \rightarrow N = \frac{F \cos 25}{\mu}$$
 (#4)

sub into (#2)

$$\frac{F \cos 25}{\mu} + F \sin 25 - mg = 0$$

$$F \left[\frac{\cos 25}{\mu} + \sin 25 \right] = mg \rightarrow F = \frac{mg}{\frac{\cos 25}{\mu} + \sin 25}$$

$$F = \frac{(50 \text{ kg})(9.8 \text{ m/s}^2)}{\frac{\cos 25}{0.20} + \sin 25} = \frac{490 \text{ N}}{4.53 + 0.42} = \boxed{99 \text{ N}}$$

b)

$$W_F = F \cdot d \cdot \cos \theta = (99 \text{ N})(20 \text{ m}) \cos(25^\circ) = \boxed{1790 \text{ J}}$$

~~b) What is work done by friction~~
 ~~$W_{\text{fric}} = F_f \cdot d \cdot \cos \theta$~~

to 2 sig. figs

$$W_F = 1800 \text{ J}$$

b) Find the work done by friction.

start with equation (#4) from part a).

$$N = \frac{F \cos 25^\circ}{\mu} = \frac{(99 \text{ N}) \cos(25^\circ)}{0.20} = \boxed{449 \text{ N}}$$

Notice this is not equal to the weight of the sled, which is 490 N. The upward pull on the sled reduces the normal force.

~~$$W = F_f \cdot d = \mu N d$$~~

$$W = F_f d \cos \theta = \mu N d \cos \theta$$

In this case θ is not the angle of the applied force.
In this case θ is the angle between the direction of motion and the direction of the frictional force.

$$W_{\text{fric}} = (0.20)(449 \text{ N})(20 \text{ m}) \cos(180^\circ) = \boxed{-1796 \text{ J}}$$

to 2 sig figs

$$\boxed{W_{\text{fric}} = -1800 \text{ J}}$$

c) What is the total work?

$$W_{\text{total}} = W_F + W_{\text{fric}} = 1800 \text{ J} - 1800 \text{ J}$$

$$\boxed{W_{\text{total}} = 0 \text{ J}}$$

Since the total work is zero, the speed of the sled remains constant.