

A wheel is initially rotating at 35π rad/s. The wheel comes to a stop after rotating through an angle of 280π rad. The moment of inertia of the wheel is 1.25 kg m². (10 pts)

- a) What is the angular acceleration of the wheel?

The provided information is

$$\omega_0 = 35\pi \text{ rad/s}$$

$$\omega_f = 0 \text{ rad/s}$$

$$\theta = 280\pi \text{ rad}$$

Using the rotational form of the fourth kinematic equation

$$\omega_f^2 - \omega_0^2 = 2\alpha \Delta\theta$$

We solve for angular acceleration

$$\alpha = \frac{\omega_f^2 - \omega_0^2}{2 \Delta\theta} = \frac{(0 \text{ rad/s})^2 - (35\pi \text{ rad/s})^2}{2 (280\pi \text{ rad})} = 6.87 \text{ rad/s}^2$$

- b) What is the torque exerted on the wheel to generate this acceleration?

Torque is related to angular acceleration through the formula

$$\tau = I\alpha$$

Since the moment of inertia is 1.25 kg m², the torque is

$$\tau = (1.25 \text{ kg m}^2) \left(6.87 \frac{\text{rad}}{\text{s}^2} \right) = 8.59 \text{ N} \cdot \text{m}$$